

Lecture 21: Texture Analysis

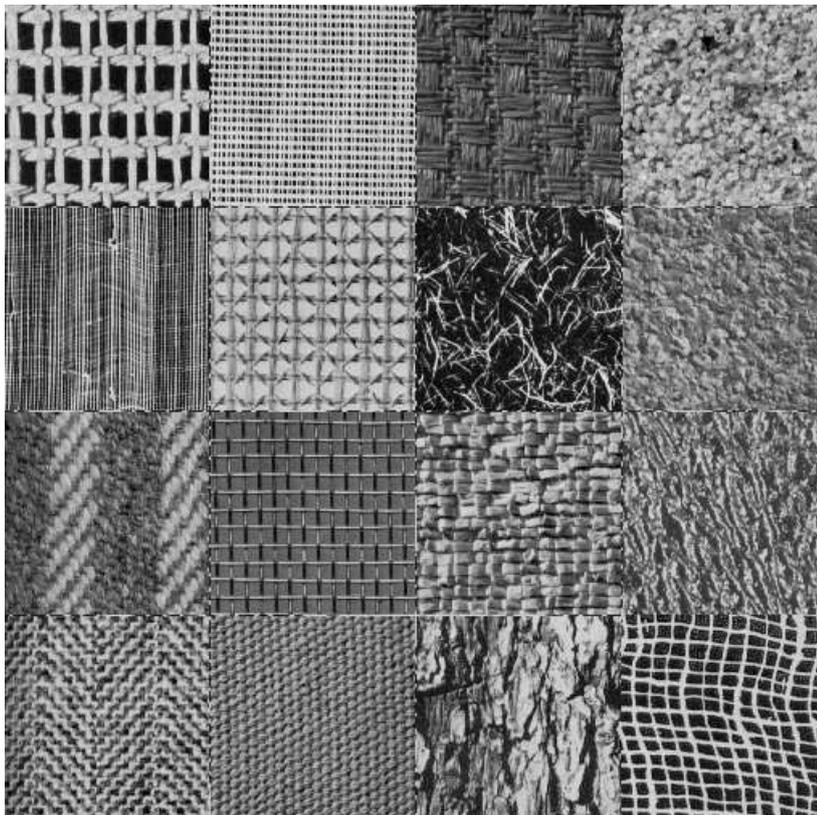
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What is Texture? (1)



16 different textures. Author: P. Brodatz (1966).

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What is Texture?

- ◆ no general formal definition
- ◆ only intuitive notion of texture:
structured region that appears in a spatially homogeneous way
- ◆ often with local stochastic fluctuations:
size, shape, colour, orientation of the underlying pattern (*textons*) may vary
- ◆ Texture analysis often applies a combination of empirically successful statistic expressions.
- ◆ Texture is a scale phenomenon.
- ◆ The eye recognises a textured region as a single object and can find segment boundaries between textured regions.

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Problems

- ◆ How can one discriminate two textures?
(Traditional edge detectors are not useful for separating two regions with different textures.)
- ◆ Is it possible to describe the complex structure of a texture with a few parameters?

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Texture Analysis without Neighbourhood Context

Often the average grey value is not sufficient for distinguishing different textures. Then better descriptors such as statistical moments may be useful.

Statistical Moments:

- ◆ Consider an image with N pixels with grey values f_1, \dots, f_N and mean μ . Then its *central moment of order k* is defined as

$$M_k := \frac{1}{N} \sum_{i=1}^N (f_i - \mu)^k.$$

- ◆ Equivalent characterisation:
For a histogram $p(z_1), \dots, p(z_L)$ where z_1, \dots, z_L are the different grey values and p their relative frequency of occurrence, the k -th central moment is given by

$$M_k := \sum_{i=1}^L (z_i - \mu)^k p(z_i).$$

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Important Examples:

- ◆ $k = 2$: *Variance (Varianz)*

$$\sigma^2 := M_2 = \frac{1}{N} \sum_{i=1}^N (f_i - \mu)^2$$

measures the fluctuations around the mean

- ◆ $k = 3$: *Skewness (Schiefe)*

$$V := \frac{1}{N} \sum_{i=1}^N \left(\frac{f_i - \mu}{\sigma} \right)^3$$

measures the assymetry:

$V < 0$: skewness towards left side.

$V > 0$: skewness towards right side.

The normalisation by σ makes different distributions comparable.

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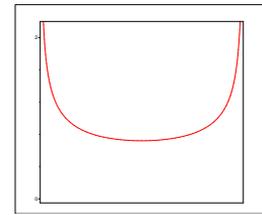
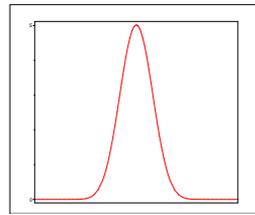
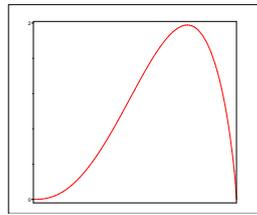
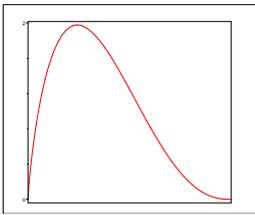
Texture Analysis without Neighbourhood Context (3)

- ◆ $k = 4$: *Excess, Kurtosis (Exzess, Kurtosis)*

$$\varepsilon := \frac{1}{N} \sum_{i=1}^N \left(\frac{f_i - \mu}{\sigma} \right)^4 - 3$$

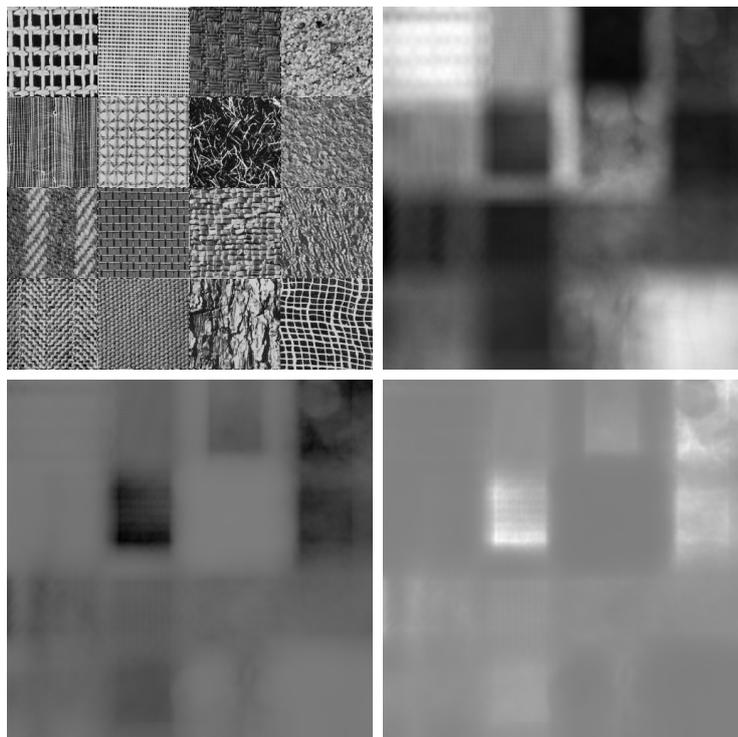
measures the flatness of the distribution:
Subtraction by 3 gives $\varepsilon = 0$ for a Gaussian distribution.

- ◆ Examples of distributions with



(a) positive skewness, (b) negative skewness, (c) positive kurtosis, (d) negative kurtosis.
Author: B. Burgeth (2005).

Texture Analysis without Neighbourhood Context (4)



(a) **Top left**: Original image, 512×512 pixels. (b) **Top right**: Variance, averaged within a disk-shaped neighbourhood of radius 30, and rescaled to $[0,255]$. (c) **Bottom left**: Skewness, rescaled. (d) **Bottom right**: Kurtosis, rescaled. Author: J. Weickert (2008).

Texture Analysis without Neighbourhood Context (4)



Texture Discrimination

- ◆ Replace every grey value by a texture attribute (e.g. a statistical moment) within some window.
- ◆ Apply a classical edge detector to the resulting image (Lectures 18 and 19).

Disadvantage of All Texture Descriptors So Far

- ◆ If one uses them for a *global* description of an image or a region, then the spatial ordering of the pixels does not matter:
A checkerboard image has the same texture descriptor as an image with a black and a white half.
- ◆ Statistics with features that ignore the spatial context is called *first-order statistics*.
- ◆ Incorporating the neighbourhood context would be desirable (*second-order statistics*).

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Texture Analysis with Neighbourhood Context (1)



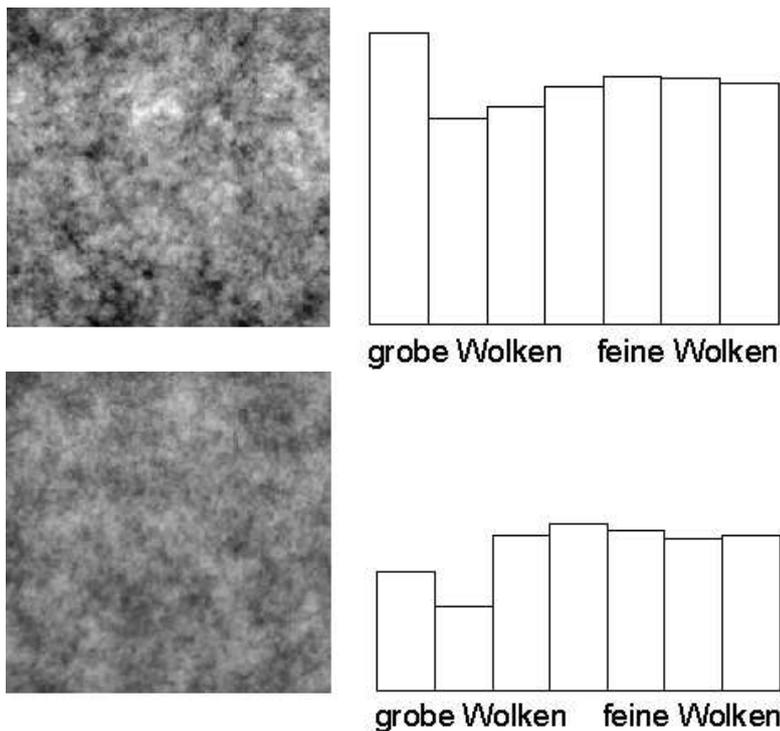
Texture Analysis with Neighbourhood Context

Possibility 1: Multiscale Representation

- ◆ Characterise the image on different scales, e.g. using
 - pyramids (Lecture 5)
Example: Analysing the cloudiness in fabrics
 - scale-space concepts (Lecture 18)
Example: Convolving the image with Gaussians of increasing standard deviation (Gaussian scale-space)
- ◆ Afterwards a texture descriptor based on first-order statistics can be used.

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Texture Analysis with Neighbourhood Context (2)



(a) **Top:** Fabric image with standard deviation σ at different scales of a pyramid representation. (b) **Bottom:** The same representation for another fabric image. Authors: J. Weickert, R. Rösch (1999).

Texture Analysis with Neighbourhood Context (3)

Possibility 2: Cooccurrence Matrices (Grauwertübergangsmatrizen, Kookkurenzmatrizen)

(Haralick et al. 1973)

- ◆ Basic idea: histogram of neighbourhood relations
- ◆ Specify some displacement vector $\mathbf{d} = (d_1, d_2)^\top$ that identifies a pair of points that is to be compared.
Example: Using $\mathbf{d} = (1, 0)^\top$ compares every pixel with its right neighbour.
- ◆ Create a bivariate grey value histogram $p_{i,j}$. It specifies the relative frequency for which some grey value i occurs together with some grey value j in direction \mathbf{d} .

2	1	2	0	1
0	2	1	1	2
0	1	2	2	0
1	2	2	0	1
2	0	1	0	1

(a)

		$P[i, j]$			
	i	0	2	2	0
	j	2	1	2	1
		2	3	2	2
		0	1	2	
		j			

(b)

(a) Left: A 5×5 image with three greyscales 0, 1 and 2. (b) Right: The cooccurrence matrix with $d = (1, 1)^T$, i.e. one considers the lower right neighbour (x axis points to the right, y axis points downwards). Example: A grey value 2 having a grey value 1 as lower right neighbour occurs in 3 out of 16 cases. Therefore, $p_{2,1} = \frac{3}{16}$. Authors: R. Jain, R. Kasturi, B. G. Schunck (1995).

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Characteristic Expressions for Cooccurrence Matrices

Many heuristically motivated expressions:

◆ Largest Probability

The maximal $p_{i,j}$ gives the most frequent grey value configuration with respect to d .

Example: In the previous image with $d = (1, 1)^T$, the configuration (2, 1) was most frequent ($p_{2,1} = \frac{3}{16}$).

◆ Contrast

$$\sum_{i,j} (i - j)^2 p_{i,j}$$

attains small values, if many grey values in the neighbourhood are similar.

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◆ *Homogeneity*

$$\sum_{i,j} \frac{p_{i,j}}{1 + |i - j|}$$

is small, if many different grey values exist in the neighbourhood.

◆ *Entropy*

$$-\sum_{i,j} p_{i,j} \log p_{i,j}$$

is a measure of randomness. It is maximal, if all possible configurations are equally probable.

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Possibility 3: Texture Analysis in the Fourier Domain

- ◆ well-suited for (almost) periodic textures
- ◆ One wants to characterise the rich information in the Fourier domain with a few parameters.
- ◆ One considers the Fourier spectrum of the textured image f in polar coordinates: $|\hat{f}(r, \phi)|$
- ◆ By integrating in circular,

$$g(r) := \int_0^{2\pi} |\hat{f}(r, \phi)| d\phi$$

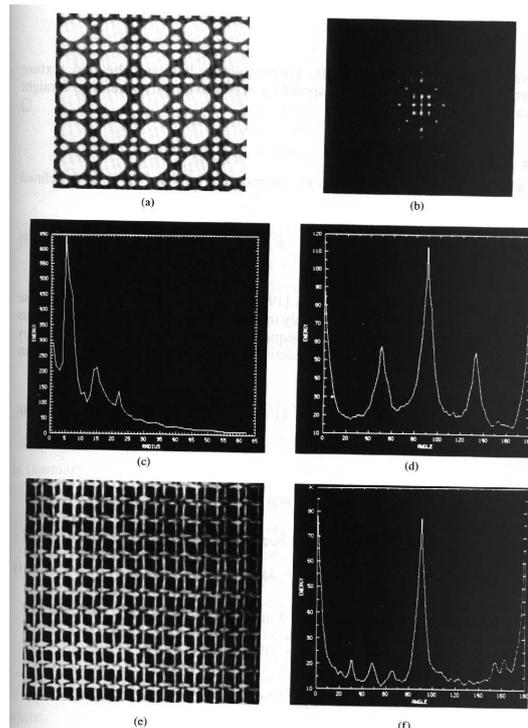
and radial direction,

$$h(\phi) := \int_0^R |\hat{f}(r, \phi)| dr$$

one obtains two functions in one variable: $g(r)$ and $h(\phi)$. They characterise the radial behaviour and the angular dependency in the Fourier spectrum.

- ◆ By computing simple expressions (e.g. maximum, mean, variance) for these functions, many textures can be discriminated.

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(a) Image with periodic texture. (b) Fourier spectrum. (c) Plot of $g(r)$. It is less conclusive. (d) Plot of $h(\phi)$. One observes diagonal structures at 45 and 135 degrees. (e) Another textured image. (f) Its $h(\phi)$ plot. Here one cannot find characteristic diagonal structures. Authors: R. C. Gonzalez, R. E. Woods (1992).

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Summary (1)

Summary

- ◆ Texture characterises reoccurring patterns, often with stochastic fluctuations.
- ◆ There is no fundamental theory for analysing textures, only several classes of heuristically motivated strategies.
- ◆ First-order statistics (e.g. moments) is usually not sufficient since neighbourhood structures are important in texture analysis.
- ◆ Simple remedy: embedding into a multiscale representation
- ◆ Cooccurrence matrices are grey value histograms of neighbourhood structures. With first-order statistics one obtains characteristic texture descriptors.
- ◆ For periodic structures, one should consider texture descriptors in the Fourier domain.

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